#### **Multi-view Stereo for 3D Reconstruction**

*Hosung Son Vision & Display Systems Lab. Dept. of Electronic Engineering, Sogang University*

## **Outline**

- Introduction
	- Usage of depth estimation
	- Two-view Stereo & Multi-view Stereo
- Background
	- Stereo Matching
	- Feature Descriptors/Matching Algorithms
	- ▪Camera Parameters
	- Homography
	- Matching Cost Volume
- MVSNet (ECCV2018)
- CVP-MVSNet (CVPR2020 Oral)
- PatchmatchNet (CVPR2021 Oral)





- Usage of depth estimation
	- AR



• Autonomous Driving

• 3D Scene Reconstruction • 3D Scanning









- Two-view Stereo
	- It is similar to Human vision system Fuses a pair of images to get sensation of depth.







• Multi-view Stereo



- Interrupted by Occlusion, Non-Lambertian, Reflection, textureless…etc.
- Number of view-points  $\square$  Sparse?
- Is deep learning-based model always better than traditional MVS algorithm?





• Quality difference between using 3 or 4 images to reconstruct each 3d points.







- Camera Poses were extracted by Structure-from-Motion(SfM). **Input images Using 3 images Using 4 images**
- Dense 3D scene was reconstructed by MVS method.





• Stereo Matching

 $x'^T E x = 0, E = R[t]_{\times}$ 

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From Epipolar constraint,







- Feature(key points) descriptors
	- Harris Corner Detector
		- Traditional Method since 1988.
		- Invariant for translation, illumination and rotation.
		- Variant for scaling.
		- Move fixed size window with 1 px







**Moving windows**

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"flat" region: no change in all directions

"edge": no change along the edge direction

"corner": significant change in all directions

• Compute SSD(Sum of Squared Difference) each state and define locally maximum min(E) as "Corner".

$$
E(\Delta x, \Delta y) = \sum_{W} [I(x_i + \Delta x, y_i + \Delta y) - I(x_i, y_i)]^2
$$
  
\n
$$
I(x_i + \Delta x, y_i + \Delta y) \approx I(x_i, y_i) + [I_x(x_i, y_i) I_y(x_i, y_i)] \left[\begin{array}{c} \Delta x \\ \Delta y \end{array}\right]
$$
  
\n
$$
E(\Delta x, \Delta y) = \sum_{W} [I(x_i + \Delta x, y_i + \Delta y) - I(x_i, y_i)]^2
$$
  
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$$
\approx \sum_{W} [I(x_i, y_i) + [I_x(x_i, y_i) I_y(x_i, y_i)] \left[\begin{array}{c} \Delta x \\ \Delta y \end{array}\right]
$$
  
\n
$$
= [\Delta x \Delta y] \left[\begin{array}{c} \sum_{W} I_x(x_i, y_i)^2 \\ \sum_{W} I_x(x_i, y_i)^2 \end{array}\right] \left[\begin{array}{c} \Delta x \\ \Delta y \end{array}\right]
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- Feature (key points) Descriptors
	- SIFT (Scale-Invariant Feature Transform)
		- · Invariant for rotation, illumination, translation, scaling.
		- · Algorithm
			- Make Scale Space  $\mathbf{1}$ .
				- 4 stages : 2x, original,  $\frac{1}{2}$ ,  $\frac{1}{4}$  size images  $\circled{1}$





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**Matching example with SIFT**

Blur and subsam

Blur and subsample

Blur and subsample

**Scale Space**

Level 4 Level 3

Level 2<br>4 resolution

Level 1

/2 resolution

Level 0 Original image



**Removing bad key points**



- Generally Blurring them with Gaussian Filtering  $(2)$
- Computing DoG(Difference of Gaussian) with 3 images in each stage  $2.$

$$
D(\mathbf{x}) = D + \frac{\partial D^T}{\partial \mathbf{x}} \mathbf{x} + \frac{1}{2} \mathbf{x}^T \frac{\partial^2 D}{\partial^2 \mathbf{x}^2} \mathbf{x}
$$

- Finding key points  $3.$
- Remove bad key points  $4.$  $R = tr(H)^2$ /det(H), If  $R > \frac{(r_{th}+1)^2}{r_{th}}$ , It is Poor.  $(r_{th}=10)$
- SURF (Speed-Up Robust Features)
	- Faster, more robust method.



**DoG Computation**

Difference of Gaussian (DOG

- Feature(key points) Matching
	- •Brute Force Matcher
		- In BF Matcher, we have to match descriptor of all features in an image to descriptors of all features in another image.
		- It is extremely expensive, however, doesn't guarantee getting an optimal solution.
	- •RANSAC (RANdom Sample Consensus)
		- Randomly choose some samples and make a model with them.
		- Compute distance and count the number of samples which loss is lower than threshold.
		- Select a model which has the maximum number of consensus iteratively.







- Camera Parameters
	- Intrinsic

$$
-K = \begin{bmatrix} f_x & \gamma & c_x & 0 \\ 0 & f_y & c_y & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix} \leftarrow \text{Camera California}
$$

· Extrinsic camera parameters

$$
-\begin{bmatrix} R_{3\times 3} & t_{3\times 1} \\ O_{1\times 3} & 1 \end{bmatrix}_{4\times 4}
$$

- $-R_{3\times 3}$ : Rotation matrix
- $-t_{3\times 1}$ : Translation vector
- Essential Matrix  $(E)$

 $E = R[t]_{\times}$ 

- Fundamental Matrix  $(F)$ 

8-point Algorithm



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**Epipolar Geometry**



• Homography

$$
\mathbf{H}_i(d) = \mathbf{K}_i \cdot \mathbf{R}_i \cdot \left( \mathbf{I} - \frac{(\mathbf{t}_1 - \mathbf{t}_i) \cdot \mathbf{n}_1^T}{d} \right) \cdot \mathbf{R}_1^T \cdot \mathbf{K}_1^T.
$$
  $s \begin{bmatrix} x \\ y' \\ 1 \end{bmatrix} = H \begin{bmatrix} x \\ y \\ 1 \end{bmatrix} = \begin{bmatrix} h_{11} & h_{12} & h_{13} \\ h_{21} & h_{22} & h_{23} \\ h_{31} & h_{32} & h_{33} \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$ 

- Homography matrix is a relation between two planar surface in space.
- There are diverse practical applications such as image rectification, registration.











**planar surface and image plane viewed by two camera positions rotating camera and image stitching**

- $\cdot$  *H* is 3 by 3 matrix with 8 DoF since it is generally normalized.
	- $h_{33} = 1$  or  $h_{11}^2 + h_{12}^2 + h_{13}^2 + h_{21}^2 + h_{22}^2 + h_{23}^2 + h_{31}^2 + h_{32}^2 + h_{33}^2 = 1$









#### • Matching Cost Volume

- Plane-sweep algorithm (aggregation function : ZNCC)
	- Map each target image  $I_k$  to the reference image  $I_{ref}$  for each depth plane  $\Pi_m$ with the homography  $H^{-1}_{\Pi_m, P_k}$  giving the warped image  $\tilde{I}_{k,m}$
	- Compute the similarity between  $I_{ref}$  and each  $\tilde{I}_{k,m}$  using Zero-mean Normalized Cross Correlation(ZNCC) between small patches W around each pixel.
	- Compute the figure-of-merit for each depth plane by combining the similarity measurements for each image  $k$

$$
M(\mathbf{u}, \mathbf{v}, \Pi_m) = \sum_{k} ZNCC(I_{ref}, \check{I}_{k,m})
$$

- For each pixel, select the depth plane with best fit

$$
\widetilde{\Pi}(u,v) = argmax M(u,v,\Pi_m)
$$

$$
\leftarrow \text{projective re-sampling of}(X, Y, Z) \leftarrow \text{projective re-sampling of}(X, Y, Z) \leftarrow \text{projective re-sampling of}(X, Y, Z) \leftarrow \text{input image}
$$
\n
$$
\text{Compute } \text{complexity} \leftarrow \text{proposite}
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 $f_i$ : i<sup>th</sup> pixel intensity of  $I_{ref}$ , f: mean of  $I_{ref}$  intensity  $g_i$ : i<sup>th</sup> pixel intensity of  $\tilde{I}_{km}$ ,  $\tilde{f}$ : mean of  $\tilde{I}_{km}$  intensity



Reference camera

 $u = K_{\text{ref}}[I \mid 0]$ 

Camera A  $u' = K_k [R_k | t_k]$  I

Comparison of Various Stereo Vision Cost Aggregation Methods : https://www.ijeit.com/vol%202/Issue%208/IJEIT1412201302\_45.pdf





**Visualization of plane sweeping**

### **MVSNet (ECCV2018)**

• Standard Multi-view Stereo Network for 3D reconstruction



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$$
\mathbf{H}_{i}(d) = \mathbf{K}_{i} \cdot \mathbf{R}_{i} \cdot \left( \mathbf{I} - \frac{(\mathbf{t}_{1} - \mathbf{t}_{i}) \cdot \mathbf{n}_{1}^{T}}{d} \right) \cdot \mathbf{R}_{1}^{T} \cdot \mathbf{K}_{1}^{T}
$$
\n
$$
\mathbf{C} = \mathcal{M}(\mathbf{V}_{1}, \cdots, \mathbf{V}_{N}) = \frac{\sum_{i=1}^{N} (\mathbf{V}_{i} - \overline{\mathbf{V}_{i}})^{2}}{N}
$$
\n
$$
\mathbf{D} = \sum_{d=d_{min}}^{d_{max}} d \times \mathbf{P}(d)
$$
\n
$$
Loss = \sum_{p \in \mathbf{p}_{valid}} \underbrace{\|d(p) - \hat{d}_{i}(p)\|_{1}}_{Loss0} + \lambda \cdot \underbrace{\|d(p) - \hat{d}_{r}(p)\|_{1}}_{Loss1}
$$

**Illustration of inferred depth map, Probability distributions and probability Map**



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## **MVSNet (ECCV2018)**

- Matching cost volume with Feature map variance
	- $\bullet$   $C = M(V_1, \cdots, V_N) = \frac{1}{N} \sum_{i=1}^N (V_i \overline{V}_i)^2$ ,  $V_i: i^{th}$  warped feature volumes
	- Setting Mean of Squared Difference to Cost volume
- Depth Refinement
	- Depth residual learning at the end of Network.
	- Use reference image as a guidance to refine the initial depth map.
	- Concatenate the <u>initial depth map</u> and resized reference image as a 4-channel input

 $\rightarrow$  Pass to the three 32-channel 2D CNN layers to learn the depth residual.

- Add the residual and initial depth map, finally generate refined depth map.
- Limitations
	- Computational Cost (GPU Memory demand : around 11GB)
	- Time consuming (takes 230s for one scan  $\rightarrow$  4.7s per view)
	- Occlusion







- Contribution
	- ▪Computational efficient depth inference network for MVS.
	- ▪Cost volume pyramid in a coarse-to-fine manner.
	- **.** 6x-faster than current SOTA & better accuracy.





#### • Cost Volume Pyramid

- Common MVS methods generate a Cost volume with fixed resolution to inference depth map.
- Instead, proposed method generate multi-level Cost volume pyramid.
- Estimate depth for each cost volumes and refine them using residual depth iteratively.
- The resolution of depth map increases generally.

 $\rightarrow$  High resolution depth map with high accuracy.

 $\bullet$  Cost volume equation at level L

$$
\mathbf{C}_d^L = \frac{1}{(N+1)} \sum_{i=0}^N (\tilde{\mathbf{f}}_{i,d}^L - \bar{\mathbf{f}}_d^L)^2
$$

• Similar to MVSNet, 3D convolution was applied to the constructed cost volume pyramid and output Depth Probability Map  $P(d)$  from softmax operation. (d: sampled depth plane)





#### • Depth Map Inference

• Coarse Depth map

$$
\mathbf{D}^L(\mathbf{p})=\sum_{m=0}^{M-1}d\mathbf{P}_{\mathbf{p}}^L(d)
$$

 $-L^{th}$  level Depth estimate for each pixel **p** 

$$
- d = d_{min} + m(d_{max} - d_{min})/M
$$
: sampled depth

• Refined Depth map

$$
\mathbf{D}^l(\mathbf{p}) = \mathbf{D}_{\uparrow}^{l+1}(\mathbf{p}) + \sum_{m=-M/2}^{(M-2)/2} r_{\mathbf{p}} \mathbf{P}_{\mathbf{p}}^l(r_{\mathbf{p}})
$$

$$
-l\in\{L-1,L-2,\cdots,0\}
$$

 $-r_p = m \cdot \Delta d_p^l$ : depth residual hypothesis ( $m \in \{0, 1, 2, \dots, M - 1\}$ ,  $M = 48$  at experiment)

- No depth map refinement after proposed pyramidal depth estimation can obtain good results.

• Loss Function

$$
Loss = \sum_{l=0}^{L} \sum_{\mathbf{p} \in \Omega} \|\mathbf{D}^{l}_{GT}(\mathbf{p}) - \mathbf{D}^{l}(\mathbf{p})\|_{1}
$$



#### • Performance



#### • Comparison of reconstruction quality



$$
f - \text{score:}
$$
\n
$$
e_{r \to g} = \min_{g \in g} |r - g|, e_{g \to \mathcal{R}} = \min_{r \in \mathcal{R}} |g - r|
$$
\n
$$
P(d) = \frac{100}{|\mathcal{R}|} \sum_{r \in \mathcal{R}} [e_{r \to g} < \text{thrs.}]
$$
\n
$$
R(d) = \frac{100}{|g|} \sum_{g \in g} [e_{g \to \mathcal{R}} < \text{thrs.}]
$$
\n
$$
F(d) = \frac{2P(d)R(d)}{P(d) + R(d)}
$$



Accuracy: Distance from estimated point clouds to the ground truth ones.

Completeness: Distance from ground truth point clouds to the estimated ones.







- Network Structure
	- ▪Refrain from parameterizing the per-pixel hypothesis as a slanted plane.
	- Instead, adaptive evaluation was used to organize the spatial pattern within the window over which matching costs are computed.
- 3-steps in Learning-based Patchmatch
	- 1. Initialization and Local Perturbation: generate random hypotheses.
	- 2. Adaptive propagation: propagate hypotheses to neighbors.
	- 3. Adaptive evaluation: compute the matching costs for all hypotheses, choose best solutions.







- Initialization
	- First, sample per pixel  $D_f$  depth hypotheses in the *inverse* depth range.

 $\rightarrow$  It helps model be applicable to complex and large-scale scenes.

- Divide the range into  $D_f$  intervals and ensure that each interval is covered by one hypothesis.
- Local Perturbation
	- Generating per pixel  $N_k$  hypotheses uniformly in the normalized inverse depth range  $R_k$ .
	- Decrease gradually  $R_k$  for finer stage.
	- Sampling around the previous estimation can refine result locally and correct wrong estimates.





- Adaptive Propagation
	- Based on Deformable Convolution Networks.

- DCN : offset based flexibly sampling along with Convolution Networks.

- To gather  $K_p$  depth hypothesis for pixel **p** in the reference image, model learns additional 2D <u>offsets</u>  $\{\Delta \mathbf{o}_i(\mathbf{p})\}_{i=1}^{K_p}$  that are applied on top of <u>fixed 2D offsets</u>  $\{\mathbf{o}_i\}_{i=1}^{K_p}$  organized as a grid.
- Apply a 2D CNN on the reference feature map  $F_0$  to learn additional 2D offsets for each pixel p.
- Depth hypotheses  $\mathbf{D}_p(\mathbf{p})$  via bilinear interpolation:







- **(a) reference image**
- **(b) Fixed sampling locations**
- **(c) Adaptive sampling locations**





- Adaptive Evaluation
	- Differentiable Warping
	- Matching cost computation
		- Group-wise correlation
			- 1.  $F_0(p)$ ,  $F_i(p_{i,j})$ : features in the ref, src feature maps. (view i, j th set of depth hypothesis)
			- divide feature maps' feature channels evenly into  $G$  groups.  $2.$
			- 3.  $\langle \cdot, \cdot \rangle$ : inner product
			- 4.  $S_i(\mathbf{p},j)^g = \frac{G}{c} \langle \mathbf{F}_0(\mathbf{p})^g, \mathbf{F}_i(\mathbf{p}_{i,j})^g \rangle \in \mathbb{R}^G : g^{th}$  group similarity (C: # of channel)
		- Pixel-wise view weight network
			- Composed of 3D convolution layers with 1x1x1 kernels and sigmoid.  $1.$
			- Takes the initial set of similarities  $S_i$  to output a number between 0 and 1 per pixel and depth hypothesis. 2.
			- $w_i(\mathbf{p}) = \max\{P_i(\mathbf{p},j)|j=0,1,\dots,D-1\}$ : view weights for pixel p and source image  $I_i$ 3.

4. 
$$
\overline{S}(\mathbf{p},j) = \frac{\sum_{i=1}^{N-1} w_i(\mathbf{p}) \cdot S_i(\mathbf{p},j)}{\sum_{i=1}^{N-1} w_i(\mathbf{p})}
$$
: final per group similarities for pixel **p** and  $j^{th}$  hypothesis

- Finally, compose  $\overline{S}(\mathbf{p}, j)$  for all pixels and hypothesis into  $\overline{S} \in \mathbb{R}^{W \times H \times D \times G}$ 5.
- Apply a small network with 3D convolution and 1x1x1 kernels to obtain single cost  $C \in \mathbb{R}^{W \times H \times D}$ 6.





- Adaptive Evaluation
	- Adaptive spatial cost aggregation
		- $-K_e$ : spatial window

object boundary textureless area

 $(b)$ 

(b) Spatial regularization



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- **(a) reference image**
- **(b) Fixed sampling locations**
- **(c) Adaptive sampling locations**





**Visualization of adaptive propagation of two typical situations**

(b) textureless region

(d) 3D CNN regularization



- $-w_k$ : feature weight at a pixel **p** based on the feature similarity.
- $-d_k$ : depth weight based on the similarity of depth hypotheses.
- Aggregated spatial cost:

$$
\tilde{\mathbf{C}}(\mathbf{p},j) = \frac{1}{\sum_{k=1}^{K_e}w_kd_k}\sum_{k=1}^{K_e}w_kd_k\mathbf{C}(\mathbf{p}\!+\!\mathbf{p}_k\!+\!\Delta\mathbf{p}_k,j)
$$

- Depth regression
	- Apply softmax to (negative) cost  $\tilde{C}$  to generate a probability **P**.
	- $-$  Regressed depth value at pixel  $\mathbf{p}$ :

$$
\mathbf{D}(\mathbf{p}) = \sum_{j=0}^{D-1} d_j \cdot \mathbf{P}(\mathbf{p}, j)
$$

 $H \times W$  $H \times W \times D$ Memory: H x W

> (c) Recurrent regularization **Cost volume regularization schemes (d) Captures context in all dimensions by using 3D CNN**





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(a) Winner-take-all

#### • Performance







**Results on DTU's evaluation set (lower is** 





